

F01BVF – NAG Fortran Library Routine Document

Note. Before using this routine, please read the Users' Note for your implementation to check the interpretation of bold italicised terms and other implementation-dependent details.

1 Purpose

F01BVF transforms the generalized symmetric-definite eigenproblem $Ax = \lambda Bx$ to the equivalent standard eigenproblem $Cy = \lambda y$, where A , B and C are symmetric band matrices and B is positive-definite. B must have been decomposed by F01BUF.

2 Specification

```
SUBROUTINE F01BVF(N, MA1, MB1, M3, K, A, IA, B, IB, V, IV, W, IFAIL)
INTEGER          N, MA1, MB1, M3, K, IA, IB, IV, IFAIL
real           A(IA,N), B(IB,N), V(IV,M3), W(M3)
```

3 Description

A is a symmetric band matrix of order n and bandwidth $2m_A + 1$. The positive-definite symmetric band matrix B , of order n and bandwidth $2m_B + 1$, must have been previously decomposed by F01BUF as $ULDL^T U^T$. F01BVF applies U , L and D to A , m_A rows at a time, restoring the band form of A at each stage by plane rotations. The parameter k defines the change-over point in the decomposition of B as used by F01BUF and is also used as a change-over point in the transformations applied by this routine. For maximum efficiency, k should be chosen to be the multiple of m_A nearest to $n/2$. The resulting symmetric band matrix C is overwritten on A . The eigenvalues of C , and thus of the original problem, may be found using F08HEF (SSBTRD/DSBTRD) and F08JFF (SSTERF/DSTERF). For selected eigenvalues, use F08HEF (SSBTRD/DSBTRD) and F02BFF.

4 References

- [1] Crawford C R (1973) Reduction of a band-symmetric generalized eigenvalue problem *Comm. ACM* **16** 41–44

5 Parameters

- 1: N — INTEGER *Input*
On entry: n , the order of the matrices A , B and C .
- 2: MA1 — INTEGER *Input*
On entry: $m_A + 1$, where m_A is the number of non-zero super-diagonals in A . Normally $MA1 \ll N$.
- 3: MB1 — INTEGER *Input*
On entry: $m_B + 1$, where m_B is the number of non-zero super-diagonals in B .
Constraint: $MB1 \leq MA1$.
- 4: M3 — INTEGER *Input*
On entry: the value of $3m_A + m_B$.
- 5: K — INTEGER *Input*
On entry: k , the change-over point in the transformations. It must be the same as the value used by F01BUF in the decomposition of B .
Suggested value: the optimum value is the multiple of m_A nearest to $n/2$.
Constraint: $MB1 - 1 \leq K \leq N$.

6: A(IA,N) — *real* array *Input/Output*

On entry: the upper triangle of the n by n symmetric band matrix A , with the diagonal of the matrix stored in the $(m_A + 1)$ th row of the array, and the m_A super-diagonals within the band stored in the first m_A rows of the array. Each column of the matrix is stored in the corresponding column of the array. For example, if $n = 6$ and $m_A = 2$, the storage scheme is

$$\begin{array}{cccccc} * & * & a_{13} & a_{24} & a_{35} & a_{46} \\ * & a_{12} & a_{23} & a_{34} & a_{45} & a_{56} \\ a_{11} & a_{22} & a_{33} & a_{44} & a_{55} & a_{66} \end{array}$$

Elements in the top left corner of the array need not be set. The following code assigns the matrix elements within the band to the correct elements of the array:

```

      DO 20 J = 1, N
        DO 10 I = MAX(1,J-MA1+1), J
          A(I-J+MA1,J) = matrix (I,J)
        10 CONTINUE
      20 CONTINUE

```

On exit: A is overwritten by the corresponding elements of C .

7: IA — INTEGER *Input*

On entry: the first dimension of the array A as declared in the (sub)program from which F01BVF is called.

Constraint: $IA \geq MA1$.

8: B(IB,N) — *real* array *Input*

On entry: the elements of the decomposition of matrix B as returned by F01BUF.

9: IB — INTEGER *Input*

On entry: the first dimension of the array B as declared in the (sub)program from which F01BVF is called.

Constraint: $IB \geq MB1$.

10: V(IV,M3) — *real* array *Workspace*

11: IV — INTEGER *Input*

On entry: the first dimension of the array V as declared in the (sub)program from which F01BVF is called.

Constraint: $IV \geq m_A + m_B$.

12: W(M3) — *real* array *Workspace*

13: IFAIL — INTEGER *Input/Output*

On entry: IFAIL must be set to 0, -1 or 1. For users not familiar with this parameter (described in Chapter P01) the recommended value is 0.

On exit: IFAIL = 0 unless the routine detects an error (see Section 6).

6 Error Indicators and Warnings

Errors detected by the routine:

IFAIL = 1

On entry, $MB1 > MA1$.


```

+           R,IBLOCK,ISPLIT,WORK,IWORK,INFO)
  IF (INFO.NE.0) THEN
    WRITE (NOUT,99999) 'sstebz', INFO
  ELSE
    WRITE (NOUT,*)
    WRITE (NOUT,*) 'Selected eigenvalues'
    WRITE (NOUT,99998) (R(I),I=1,M)
  END IF
END IF
END IF
STOP
*
99999 FORMAT (1X,'INFO from ',A6,' = ',I3)
99998 FORMAT (1X,8F9.4)
END

```

9.2 Program Data

F01BVF Example Program Data

```

9  2  2
11
12  12
13  13
14  14
15  15
16  16
17  17
18  18
19  19
101
22  102
23  103
24  104
25  105
26  106
27  107
28  108
29  109
1  3

```

9.3 Program Results

F01BVF Example Program Results

```

Selected eigenvalues
-0.2643 -0.1530 -0.0418

```
